$\qquad$

## Scatter Plots display data in two variables．

Data points are plotted on a graph to represent data and determine correlation．
Scatter Plots may show positive，negative，or no correlation．

Positive correlation means when one variable increases，so does the other．
Negative correlation means that when one variable increases，the other decreases．
No correlation means that the data appear unrelated．

Practice：Label the correlation that you suspect would be demonstrated by each：
（pos．，neg．，or no）

1．Height versus weight of 100 male African elephants．

2．Distance driven versus gas used．

3．Amount of time spent studying versus G．P．A．

4．Hair length versus height of 150 adult women．

5．Distance walked in a pair of shoes versus the thickness of the sole．

On a graph，it is easy to recognize the correlation：


The trend line for a scatter plot is called the Best Fit Line or Line of Best Fit and can be described as a linear equation in slope－intercept form．


Creating a scatter plot is easy once the graph is drawn.
Practice: The Data Below shows the average test scores in California on the standardized Reading and Math tests for 8 years from 1992-1999. Create a Scatter Plot to display the data.

| Year | Math Score | Reading Score |
| :--- | :--- | :--- |
| 1992 | 32 | 38 |
| 1993 | 40 | 39 |
| 1994 | 50 | 55 |
| 1995 | 48 | 48 |
| 1996 | 39 | 46 |
| 1997 | 45 | 50 |
| 1998 | 42 | 45 |
| 1999 | 40 | 47 |



Creating a scatter plot is more difficult when you must create your own graph.
Practice: The Data Below shows the height and weight of 12 female students in Mrs. Phillips' first grade class. Label the graph so that the data fits and plot the points below.

## Height versus Weight

| Name | Height | Weight |
| :--- | :--- | :--- |
| Lisa | 44 | 47 |
| Simone | 50 | 57 |
| Meredith | 38.5 | 32 |
| Penny | 39 | 42 |
| Sheila | 41 | 36 |
| Tara | 45.5 | 49 |
| Meg | 48 | 62 |
| Mara | 51 | 47 |
| Steph | 53 | 65 |
| Callie | 50.5 | 49 |
| Cynthia | 46.5 | 52 |
| Joy | 45 | 43 |



Using the data from Mrs. Phillips' first grade class, we will use the graphing calculator to display the data and determine the line of best fit.

Clear the memory of your calulator before starting.

1. Enter the data. Choose STAT and select 1: Edit...

Enter the height data under L1 and the weight data under L2.

| Name | Height(L1) | Weight(L2) | Name | Height(L1) | Weight(L2) |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Lisa | 44 | 47 | Meg | 48 | 62 |
| Simone | 50 | 57 | Mara | 51 | 47 |
| Meredith | 38.5 | 32 | Steph | 53 | 65 |
| Penny | 39 | 42 | Callie | 50.5 | 49 |
| Sheila | 41 | 36 | Cynthia | 46.5 | 52 |
| Tara | 45.5 | 49 | Joy | 45 | 43 |

Tips:
Make sure all of the data lines up properly.
If you need to delete an entry use DEL. To insert a missing entry use INS (2nd DEL).

## 2. Plot the data.

Choose STAT PLOT (2nd Y=)
Select 1: Plot 1...
Turn the graph On. (highlight On and hit Enter)
Note the other settings, we will not change these.
ZOOM 9: ZoomStat

## 3. Calculate the Line of Best Fit

Push the STAT button. This time toggle right to CALC in the menu.
Select 4: LinReg ( $a x+b$ ) This will calculate an equation in the form $y=m x+b$. Hit ENTER.
(If you did everything correctly so far, you should have gotten $a=1.652$ and $b=-27.573$ ).

## 4. Plot the Line of Best Fit

Go to $Y_{1}=$ and then hit VARS.
Choose 5: Statistics...
Toggle right to EQ and select 1: RegEQ and GRAPH.
You may also enter the equation manually, but it will not be as accurate in most cases.

## 5. Trace the Line of Best Fit

Hit TRACE. Use the left and right arrows to bounce from point to point. Use the down arrow to toggle onto the line (not the points).

Answer: Round to the tenth.
How much would you expect a first grade girl to weigh for each height given below?
40in $\qquad$ lbs

42in $\qquad$ lbs

45in $\qquad$ lbs

48in $\qquad$ lbs

50in $\qquad$ lbs

53in $\qquad$ lbs
hint: Discover the TABLE function on your own.

Use each table of data to create a graph and a line of best fit on your calculator to answer the questions that follow.

Latitude and Average Daily Temperature in July for $\mathbf{1 0}$ world cities

| Name | Latitude ( ${ }^{\circ}$ N) | July Temp. ${ }^{\circ}$ C $\mathbf{C}$ ) |
| :--- | :--- | :--- |
| Oslo | 59 | 7 |
| Berlin | 52 | 18.5 |
| London | 51 | 17 |
| Vancouver | 49 | 17 |
| Tunis | 37 | 26 |
| Tomsk | 56 | 18 |
| Kiev | 50 | 20 |
| Coppermine | 67 | 10 |
| Rome | 41 | 24 |
| Salah | 27 | 37 |

1. What is the linear equation that represents the J uly temperature of a city based on its north latitude?
(Round decimals to the thousandth 0.001)
2. What would be the expected J uly temperature at each of the given latitudes below?
$25^{\circ} \mathrm{N}$ $\qquad$ ${ }^{\circ} \mathrm{C}$
$54{ }^{\circ} \mathrm{N}$ $\qquad$ ${ }^{\circ} \mathrm{C}$
$70^{\circ} \mathrm{N}$ $\qquad$ ${ }^{\circ} \mathrm{C}$

Latitude and Average Daily Rainfall in July for 10 world cities

| Name | Latitude ( ${ }^{\circ} \mathrm{N}$ ) | July Rainfall (mm) |
| :--- | :--- | :--- |
| Oslo | 59 | 73.6 |
| Berlin | 52 | 57.4 |
| London | 51 | 59.5 |
| Vancouver | 49 | 31.3 |
| Tunis | 37 | 3.3 |
| Tomsk | 56 | 73.6 |
| Kiev | 50 | 77.1 |
| Coppermine | 67 | 31.9 |
| Rome | 41 | 16.3 |
| Salah | 27 | 0.1 |

1. Write the equation (to the thous.):
2. What would be the expected J uly rainfall at each of the given latitudes below?
$35^{\circ} \mathrm{N}$ $\qquad$ mm
$45^{\circ} \mathrm{N}$ $\qquad$ mm
$60^{\circ} \mathrm{N}$ $\qquad$ mm
3. Does this graph appear to show more or less correlation than the one above? $\qquad$

Use each table of data to create a graph and a line of best fit on your calculator to answer the questions that follow.

Global Temperature by Year 1900-2000

| Year | Temp. ( ${ }^{\circ}$ F) |
| :---: | :---: |
|  |  |
| 1900 | 57.20 |
| 1910 | 56.82 |
| 1920 | 56.97 |
| 1930 | 57.13 |
| 1940 | 57.47 |
| 1950 | 56.93 |
| 1960 | 57.16 |
| 1970 | 57.27 |
| 1980 | 57.67 |
| 1990 | 58.08 |
| 2000 | 57.92 |

1. Write the Linear equation (to the thous.):
2. According to this (very limited) data, predict the mean global temperature for the following years.
(Use TBLSET and TABLE, or change your WI NDOW values and use TRACE)

2010 $\qquad$ 2025 $\qquad$ 2050 $\qquad$ 2100 $\qquad$

North American Population 1986-1995

| Year | Population (millions) |
| :--- | :--- |
| 1986 | 346 |
| 1987 | 350 |
| 1988 | 354 |
| 1989 | 358 |
| 1990 | 363 |
| 1991 | 369 |
| 1992 | 374 |
| 1993 | 379 |
| 1994 | 383 |
| 1995 | 388 |

3. Write the Linear equation (to the thous.):
4. Calculate and graph the Exponential Equation (Stat - Calc - ExpReg) AND the Linear Equation. What does each predict for the North American population for the year 1900?

Exponential $\qquad$ million

Linear $\qquad$ million
5. What is wrong with the linear prediction? $\qquad$

Use each table of data to create a graph and a line of best fit on your calculator to answer the questions that follow.

Made-Up Meaningless Statistical Data Table 1
Age (years) Length (cm)

| 15 | 143.6 |
| :--- | :--- |
| 20 | 140.7 |
| 25 | 132.9 |
| 30 | 133.7 |
| 35 | 129.1 |
| 40 | 108.9 |
| 45 | 109.1 |

6. What is the slope of the line of best fit to the hundredth? $\qquad$
7. What is the length at age 0 according to this equation? $\qquad$ cm
8. Predict the length at age 100 : $\qquad$ cm

## Made-Up Meaningless Statistical Data Table 2

| X: | 10 | 11 | 16 | 7 | 4 | -5 | 1 | -3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y :}$ | -2 | -1.5 | 1 | -3.5 | -5 | -9.5 | -6.5 | -8.5 |

9. What equation does this table represent (in slope-intercept form)? $\qquad$
10. What is the value of $y$ when $x=100$ ? $\qquad$

Made-Up Meaningless Statistical Data Table 3

| $\mathbf{X}:$ | 6.1 | 8.7 | 9.9 | 10.1 | 11.0 | 12.9 | 15.1 | 17.3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y :}$ | 19.3 | 6.1 | 3.2 | 3.5 | 2.8 | 1.5 | 0.3 | 0.1 |

11. Write the linear equation for the line of best fit (to the hundredth). $\qquad$
12. Write the exponential equation for the line of best fit (to the hundredth). $\qquad$
13. Which of the two equations above better fits the data given? $\qquad$
Made-Up Meaningless Statistical Data Table 4
14. Fill-in the missing data point in the table below.

| $\mathbf{X}:$ | 7.2 | 8.9 | 9.1 | 18.7 | 21.9 | 32.2 | 35.8 | 41.1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y :}$ | 23.1 | 29.1 | 29.9 | 63.1 | 74.5 |  |  | 123.2 |
|  | 142.1 |  |  |  |  |  |  |  |

$\qquad$
$\qquad$

## We have generally dealt with three types of data:

Linear data points form a straight line with a slope and intercepts.
Quadratic data forms a parabola with a vertex and (sometimes) roots).
Exponential data forms a 'ramp' with increasing slope.
You should be able to identify data types without a calculator in many cases.

## Identify each table of data as linear, quadratic, or exponential:

1. 

| $\mathbf{X}:$ | -2 | 4 | 10 | 16 | 22 | 28 | 34 | 40 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y :}$ | -9 | -10 | -11 | -12 | -13 | -14 | -15 | -16 |

2. 

| $\mathbf{X}:$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y :}$ | 1 | 2 | 4 | 8 | 16 | 32 | 64 | 128 |

3. 

| X: |
| :--- |
| X: |
| $\mathbf{Y :}$ |
|  |
|  |

4. 

| $\mathbf{X}:$ | 5 | 7 | 9 | 11 | 13 | 15 | 17 | 19 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y :}$ | 1.64 | 1.05 | .67 | .43 | .27 | .18 | .11 | .07 |

## Coefficient of Correlation

The coefficient of correlation is a number between -1 and 1 which describes how well the equation 'fits' the data. It only works for linear and exponential data and can be found using the VARS - Statictics - EQ - r menu.
A value close to 1 or -1 means there is a strong correlation.
$A$ value close to 0 means very weak correlation.
5. Calculate the linear equation for \#4 (to the thousandth): $\qquad$
6. Calculate the coefficient of correlation (to the thousandth): $\qquad$
7. Calculate the exponential equation for \#4 (to the thousandth): $\qquad$
8. Calculate the coefficient of correlation (to the thousandth): $\qquad$

## Practice:

| $\mathbf{X}:$ | -5 | -2 | 6 | 9 | -8 | 11 | 7 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y :}$ | 1.9 | 2.5 | 5.3 | 7.2 | 1.2 | 8.1 | 6.0 | 4.4 |

5. Calculate the linear equation (to the hundredth): $\qquad$
6. Calculate the coefficient of correlation (to the hundredth): $\qquad$
7. Calculate the exponential equation (to the hundredth): $\qquad$
8. Calculate the coefficient of correlation (to the hundredth): $\qquad$

Practice:

| X: | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y :}$ | 29 | 22 | 13 | 8 | 5 | 4 | 5 | 8 |

9. Calculate the linear equation (to the hundredth): $\qquad$
10. Calculate the coefficient of correlation (to the hundredth): $\qquad$
11. Calculate the exponential equation (to the hundredth): $\qquad$
12. Calculate the coefficient of correlation (to the hundredth): $\qquad$
13. Calculate the coefficient of correlation (to the hundredth): $\qquad$
14. Calculate the quadratic equation (to the hundredth): $\qquad$
15. Which of the three equations (Linear, Exponential, or Quadratic) fits the data? $\qquad$
16. If $x=10$, what will $y=$ ? $\qquad$

## Practice:

| $\mathbf{X :}$ | -3 | -8 | 19 | 4 | -1 | 30 | 14 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{Y :}$ | 7 | 23 | 102 | 21 | 12 | 145 | 54 | 32 |

16. Calculate the linear equation (to the hundredth): $\qquad$
16b. Graph the linear equation for $Y_{1}$
17. Calculate the coefficient of correlation (to the hundredth): $\qquad$
18. If the data is linear and $x=10, y=$ (to the hundredth): $\qquad$
19. Calculate the exponential equation (to the hundredth): $\qquad$
19b. Graph the exponential equation for $Y_{2}$
20. Calculate the coefficient of correlation (to the hundredth): $\qquad$
21. If the data is exponential and $x=10, y=$ (to the hundredth): $\qquad$
22. Calculate the quadratic equation (to the hundredth): $\qquad$
22b. Graph the quadratic equation for $\mathrm{Y}_{3}$
23. If the data is quadratic and $x=10, y=$ (to the hundredth): $\qquad$
24. Based on the graphs, which data point makes the data appear quadratic? ( $\qquad$ , $\qquad$ )
