Name

Divisibility Rules



Period

- A **Prime Number** is a whole number whose only factors are 1 and itself. To find all of the prime numbers between 1 and 100, complete the following exercise:
- 1. Cross out 1 by **Shading** in the box completely.
 - 1 is neither prime nor composite. It has only 1 factor itself.
- 2. Use a forward **Slash** \ to cross out all multiples of 2, starting with 4. 2 is the first prime number.
- 3. Use a backward **Slash** / to cross out all multiples of 3 starting with 6.
- 4. Multiples of 4 have been crossed out already when we did #2.
- 5. Draw a Square on all multiples of 5 starting with 10. 5 is prime.
- **6.** Multiples of 6 should be X'd already from #2 and #3.
- 7. Circle all multiples of 7 starting with 14. 7 is prime.
- 8. Multiples of 8 were crossed out already when we did #2.
- 9. Multiples of 9 were crossed out already when we did #3.
- **10.** Multiples of 10 were crossed out when we did #2 and #5.

All of the remaining numbers are prime.

How many prime numbers are left between 1 and 100?

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Answer: use your chart for help.

Is 51 prime? If not, what are its factors?

Is 59 prime? If not, what are its factors?

Is 87 prime? If not, what are its factors?

Is 91 prime? If not, what are its factors?

Name_

Divisibility Rules

There are some easy tricks you can use to determine if a number is divisible by 2, 3, 4, 5, 6, 8, 9 and 10.

A number is divisible by:

- 2 if it is even.
- **3** if the sum of its digits is divisible by 3.
- 4 if the number formed by the last 2 digits is divisible by 4.
- **5** if the ones digit is 5 or 0.
- 6 if it is divisible by 2 AND 3. (All even multiples of 3.)
- 7 there is no good trick for 7.
- 8 if the number formed by the last 3 digits is divisible by 8.
- 9 if the sum of the digits is divisible by 9.
- **10** if the last digit is a 0.
- **11:** We will learn this trick separately.

Practice: Write yes or no in each blank.

Determine whether 21,408 is divisible by:

- 2 ____ 6 ____
- 3 ____ 8 ____
- 4 ____ 9 ____
- 5 ____ 10 ____

Determine whether 1,345,866 is divisible by:

- 2 ____ 6 ____
- 3 ____ 8 ____
- 4 ____ 9 ____
- 5 ____ 10 ____

Determine whether 222,222,225 is divisible by:

- 2 ____ 6 ____ 3 - ____ 8 - ____
- 4 ____ 9 ____
- 5 ____ 10 ____

Write the complete prime factorization for each number below.Use a factor tree if necessary:Ex: 1,6001. 2102. 2973. 192

$$=2^6\cdot 5^2$$

_Period __



GCF and LCM

The GCF is the Greatest Common Factor between two or more numbers.

9.0

Algebra

Sometimes the GCF is obvious:

Find the GCF for each pair of numbers.**1.** 50 and 75**2.** 49 and 56**3.** 45 and 60

When the GCF is not obvious: **Ex.** Find the GCF between 405 and 585.

 $405 = 3 \cdot 3 \cdot 3 \cdot 3 \cdot 5$

 $585 = 3 \cdot 3 \cdot 5 \cdot 13$ Common factors are $3 \cdot 3 \cdot 5 = 45$, the GCF is 45.

notes:

The GCF between a pair or set of numbers is the product of their common prime factors.

Practice:

Find the GCF.

1. 108 and 126 **2.** 154 and 210 **3.** 108 and 288

The LCM is the Least Common Multiple. This means the smallest number that both numbers divide with no remainder.

The LCM is rarely obvious:

Find the LCM for each pair of numbers. **1.** 5 and 7 **2.** 10 and 15 **3.** 16 and 24

When the LCM is not obvious:

Ex.

Find the LCM between 144 and 168.

 $144=2\cdot 2\cdot 2\cdot 2\cdot 3\cdot 3$ Shared factors are $2\cdot 2\cdot 2\cdot 3\cdot 3$...

 $168 = 2 \cdot 2 \cdot 2 \cdot 3 \cdot 7$ other factors are $2 \cdot 3 \cdot 7 \dots$ so

 $GCF = 2 \cdot 2 \cdot 2 \cdot 3 \cdot 2 \cdot 3 \cdot 7 = 1,008$

GCF and LCM: Venn Diagrams

Algebra 9.0

Review Practice: Find the <u>GCF and LCM</u> for each:

1. 36 and 168 **2.** 28, 42, and 105

Venn Diagrams are a great way to solve GCF and LCM problems.

Example: Use a Venn diagram to find the GCF and LCM between 84 and 140.



Example: Use a Venn diagram to find the GCF and LCM for 75 and 105:

Practice: Use a Venn diagram to find the GCF and LCM for each.

1. 45 and 60 **2.** 80 and 112 **3.** 28, 42, and 105

	Name	Period
GCF and LCM Find the <u>GCF and LCM</u> for each You may use a calculator, and Ver	pair or set of numbers: In diagrams are encoura	Algebra 9.0
1 E4 and 00	a 00 and 12/	.gea .co
1. 54 and 80	2. 88 and 136	
GCF LCM	GCF LCM _	
3 . 90 and 105	4 . 45 and 72	
GCF LCM	GCF LCM _	
5. 96 and 160	6. 153 and 180	
GCF LCM	GCF LCM _	
7 . 20 and 40	8. 64 and 88	
GCF LCM	GCF LCM _	
9. 270 and 351	10. 143 and 221 (neit	her one is prime)
	0.05	
GCF LCM	GCF LCM _	

Factoring the GCF

You can find the GCF of expressions which include variables and exponents:

Algebra

2. $25x^4 - 45x^3 + 15x^2$

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Examples:

- 1. Find the GCF of $72x^5y^2$ and $120x^3y^7$:
- **2.** Find the GCF of $93a^{3}b^{11}$ and $124a^{5}b^{7}$:

Practice: Find the GCF for each pair or set:

 1. $15x^{10}$ and
 2. $78m^3n^4$ and
 3. $28a^2b$ and

 $25x^{20}$ $130m^5n$ $21ab^2$ and

 $30a^2b^2$ $30a^2b^2$

We have learned to Factor. Factoring is like Reverse Distribution.

To factor an expression:

- a. Look for the GCF of all terms, including the variables.
- b. Place the GCF outside of the parenthesis.
- c. Divide each original term by the GCF to get the terms inside the parenthesis.

Examples: Factor each.

1. 57 $x^2 - 152 xy$ 2. $110x^5 y^{10} - 132x^{15} y^5$

Practice: Factor each.

1. $160 x^3 y - 96 x^2 y^2$

Practice: Factor each.

1. $65x^{3}y - 91x^{2}y + 13xy$ 2. $44x^{40}y^{7} - 144x^{10}y^{2}$

Name

Period _____



Factoring the GCF

For each polynomial, factor the GCF from the expression. These should be easy enough to factor the GCF in your head.

- 1. $18x^3 24x$
- **2**. $3a^3 6a^2b + 9ab^2$
- **3**. 16a 32ab + 20b
- 4. $14m^5 28m^3 + 12m^2$
- 5. $10a^3 8a^2b^2 + 14a^2b$
- 6. $8x^2y 18x^2 + 12xy^2$
- 7. $30xy^4 20xy^3 15xy^2$

1.	
2.	
3.	
4.	
5.	
6.	
7.	

Name

Period _____



Factoring the GCF

For each polynomial, factor the GCF from the expression. You will likely need to find the GCF separately with these problems.

8. $80x^3 - 64x$

9. $52a^3 - 68a^2b + 60ab^2$

10. $70a^2 - 56ab + 42b^2$

11. $60m^5 - 48m^3 + 108m^2$

12. $95a^9b^8 - 70a^6b^{12}$

13. $38x^2y - 57x^2 + 76xy^2$

8. _____ 9. _____ 10. _____ 11. _____ 12. _____ 13. _____

Polynomials

A **polynomial** is a sum of one or more terms called **monomials**.

Examples:
$$x + y = 2x^3 - xy + 4y = 12x^3$$

A monomial is the product of variables and constants (numbers).

Examples: $2abc^{3}$ x^{7} $-\frac{5}{7}x$

A **binomial** is the sum of two monomials.

Examples:
$$2a^2 + a$$
 $x^2 - 3$ $\frac{2}{3}x^4 - 5x^2$

A trinomial is the sum of three monomials.

Examples:
$$2a - b + c$$
 $x^7 - y^5 - 3$

The degree of a monomial is the sum of the exponents of its variables.

Examples: $2a^2 2^{nd}$ degree $5ab^6c = 1+6+1 = 8^{th}$ degree note: The degree of a constant is zero.

The degree of a polynomial is the largest degree of its monomial terms.

Examples: $2a^2 - 7a$ is a 2nd degree binomial $5a^5 + 2b^2 - 3c$ is a 5th degree trinomial

Polynomials

Ordering Polynomials:

The general rule for ordering a polynomial is to write the terms in descending order by powers of a given variable:

Example: Arrange by descending powers of x:
$$2x + x^3 - 5 - 3x^5$$

Example: Arrange by descending powers of x: $xy + xy^2 - x + y$

Practice:

Order the following polynomials by descending powers of x.

- 1. $5xy 3x^2 x^3 + 2xy^2$ 2. $3x^2 + 4x^3y^2 + 5x^2y^3$
- 3. $ax^2 ax^3 a^3x + a^2$ 4. $7 + 2x x^3y + x^5$

Answer:

What degree is each of the polynomials above?

Other tiebreakers: Alphabetical order.

Ex: Arrange by descending powers of a: $2a^3c^2 + a^3b - 5a^3b^2 - 3a^3c$

Practice:

Order the following polynomials by descending powers of a.

1.
$$-3ab+a^{2}-c^{2}+2b^{2}$$

2. $3a^{2}+a^{3}b+5a^{2}b^{3}-a^{3}c^{2}$
3. $ax^{2}-ax^{3}-a^{3}y+a^{2}y$
4. $7az^{2}+3ax-2ay^{2}+a$

Multiplying Polynomials



Find the area of each rectangle below:





Multiplying Binomials:

Setup a grid like the one above to solve the following:

- 1. (x + 3)(x + 5) 2. (2x + 5)(x 2)
- The FOIL Method: First ac Outer ad Inner bc Last bd (a+b)(c+d) = ac+ad+bc+bd

Examples: Expand each using the FOIL Method.

1. (a + 1)(a - 3) 2. (2x - y)(3x + y)

Practice: Expand each using the FOIL Method.

- 1. (x + 3)(x 5) 2. (2a c)(3a + c)
- 3. (1-2a)(3-a) 4. $(x^2 y^2)(x+4)$

Multiplying Polynomials

Find the area of each rectangle below:



Multiplying longer polynomials is easier using the grid method: Setup a grid like the one above to solve the following: Remember to combine like terms and place answers in descending order.

1. (x+y+3)(y+5) 2. (2a+5b-3)(a-b+2)

Practice:

Expand each.

1. (x+y+3)(y+5) 2. (2a+5b-3)(a-b+2)

Practice:

Express the area of the shaded region below as a polynomial in simplest form:



Beyond the Grid

Once you have learned the grid and FOIL methods, you should begin to see multiplying polynomials is just distribution.

Examples:

1.
$$(x+y)(2x-y+5)$$
 2. $(5a-4b)(2a-3b+1)$

Practice:

Multiply each.

1. (x-2y)(x+y+5) 2. (a-2b)(2a+3b-4)

Now, multiply each using the Distributive Property. You should notice something about the answers.

1. (3x-2y)(x+5y)2. a(2a-b)-6b(2a-b)3. 3x(x+5y)-2y(x+5y)4. (a-6b)(2a-b)

Work Backwards: write each as a product of binomials.

- **1.** x(2x+3) y(2x+3) **2.** a(2a+3b) 2b(2a+3b)
- **3.** 2x(x+3y) 5(x+3y) **4.** 2a(a-7) 5b(a-7)

Use the grid method when problems get more complex:

1. (x-2y+5)(2x+3y-2) 2. $(a^3-2a^2+5a)(a^2+3a-2)$

Special Cases

Multiply each pair of binomials using the FOIL Method. Simplify answers.

1. (x + 3)(x + 5)2. (a + 5b)(2a - 3b)3. (x + 3)(x - 3)4. (a + 5b)(a - 5b)5. (x + 3)(x + 3)6. $(a - 5b)^2$

#1 and #2 are typical trinomials.#3 and #4 are called DIFFERENCE OF SQUARES. Why?#5 and #6 are called PERFECT SQUARE trinomials.

More practice: Difference of Squares. Solve each using FOIL, try to recognize a shortcut.

1. (2x-3)(2x+3)2. (2a+3b)(2a-3b)3. $(x^2+5x)(x^2-5x)$ 4. $(a^3+3)(a^3-3)$

How do you recognize a difference of squares?

More practice: Perfect Squares. Solve each using FOIL, try to recognize a shortcut.

- **1.** $(2x-3)^2$ **2.** $(2a+3b)^2$
- **3.** $(x^2 + 5x)^2$ **4.** $(a^3 3)^2$

Challenge: Expand (a-b)(a-b)(a+b)(a+b) in 1 minute.

Quiz Review

Factor out the GCF for each trinomial.

100.
$$15x^3y^2 - 20x^2y^2 + 10xy^3$$

200.
$$108a^4b^2 + 135a^4b - 36a^2b^2$$

зоо.
$$136a^3x - 72ax^2 + 48ax$$

400.
$$119x^3 - 68x^2 + 187x$$

Multiply each:

Order your answers by descending powers of x or a.

100.
$$2xy(x-3y) + 3x(x^2 - xy)$$

200.
$$(2a^2+b)(b^2-a)$$

$$x^{2}+5x-3(x^{2}-4x)$$

400.
$$(a-3b+c)(2a+2b-c)$$

Multiply each.

Order your answers by descending powers of x or a.

100. (30+3)(30-3)200. $(a+5b)^2$ 300. $(x^4-3x^3)(x^4+3x^3)$ 400. $(a^2-3)^2(a^2+3)^2$

Algebra 9.4

Factoring and FOIL Practice Quiz Factor each expression (Reverse distribution):	Algebra	9.4
1. $42x^3y^3 - 21x^2y^4 + 30xy^5$	1	
2. $48a^5b^3 - 80a^4b^2$	2	
3. $57x^6y^2 - 95x^5y + 152x^4$	3	

Name_____Period _____

9. _____

Simplify each

(Distribute, combine like terms, and then reorder the terms by descending powers of x or a):

- 4. $4(x^{2}y xy) + x(xy 3y)$ 5. ab(a+3) - 2a(4-b-5ab)6. $x^{2}(2xy - x^{2}) - 2(x-7)$ 6. ______ Multiply (FOIL or Grid method) 7. $(x^{2} - 4)(x + 3)$ 8. (a-3)(2-a)8. _____ 8. _____
- 9. (3x-2)(x-y)

	Name	Period
Factoring and FO	IL Practice Quiz	Algebra 9.4
10. $(x + y)(x - y)$		10
11. $(2a + 3)^2$		11
12. (3+2 <i>a</i>)(3-2 <i>a</i>)		12
13. $(2x + y^3)(2x - y^3)$)	13
14. (2 <i>a</i> + <i>b</i>)(2 <i>a</i> + <i>b</i>)(2	(a-b)	14
15. $(3+2x)^2$		15
16. $[(x-1)(x+1)$		

16. _____

Polynomial Applications

A common use for multiplying polynomials involves finding area.

Example: Express the area of the shaded regions in terms of x.



I will call these 'frame' problems because the diagrams usually look like frames.

Practice: Express the area of the shaded regions in terms of x.





Polynomial Applications

Word problems can involve similar area problems, but the diagrams must be given.

Example:

You are matting a photograph that is twice as tall as it is wide. You want to have five inches of matting around the entire photograph. Express the area of matting you will need based on the width (w) of the photograph.

Example:

Barry bought a new rectangular rug for his rectangular dining room. The rug is three feet longer than it is wide. The room is six feet wider than his rug, and seven feet longer than the rug. Express the area of bare floor that will be showing in terms of the rug's width (w).

Answer: If there are 190 square feet of bare floor showing, what ar the dimensions of the rug?

Practice:

Jeremy has a backyard pool surrounded by a tiled walkway that is two yards wide. The pool is 5 yards longer than it is wide. Express the area of the walkway in terms of the width (w) of the pool.

Answer: If the walkway is 196 square yards, how long is the pool?

Practice:

A painting has a frame that is 7 inches wider and 8 inches taller than the artwork it surrounds. The artwork is 5 inches taller than it is wide. Express the area of the frame in terms of the painting's width (w).

Answer: If the area of the frame is 196 square inches, what is the height of the painting?

Name_

Polynomial Applications

Express the area of each shaded region in terms of x.



Express the area of each shaded region in terms of x. 4. 5.







9.

Algebra

Name

Polynomial Applications

Algebra 9.4

Solve each. Include a sketch for each.

7. Connor is planting a garden surrounded by 1-foot square concrete blocks. The garden will be 10 feet longer than it is wide. Express the number of square blocks he will need based on the width (w) of the garden.

If he uses 56 blocks, how many square feet is the area enclosed by the blocks? _____

8. Kerry takes a sheet of paper that is 3 inches shorter than it is wide. He cuts a hole out of the paper that leaves 2 inches of paper on all sides of the hole. Express the area of the *remaining* paper rectangle in terms of w, the width of the original sheet.

If there are 52in² of paper remaining, what were the dimensions of the cut-out hole?

9. A company manufactures windows that are 30 inches taller than they are wide. The window comes with an aluminum frame that is 6 inches wide on three sides, and 10 inches wide at the bottom. Express the area of the aluminum frame in terms of the window's width (w).

Standard Form and Factoring

Algebra 9.5

A Quadratic Equation written as a function looks like this:

 $y = Ax^2 + Bx + C$ We will call this Standard Form.

Examples: List values for A, B, and C:

$$y = 2x^2 + 3x - 5$$
 $y = x^2 + 5x$

When you multiply a pair of (1st degree) binomials, you get a quadratic expression.

$$(x+3)(x-5) = x^2 - 2x - 15$$

Think!

In the equation above, what are the A, B, and C values? How did we get the values for B and C?

Factoring: Easy ones.

Today we will learn to factor simple quadratics by reversing the FOIL method.

Review: Multiply (x+2)(x+4)

$$x^{2} + 6x + 8$$
 Factoring:
Find two numbers which can be added to get 6
and multiplied to get 8.

More Examples: Factor.

1.
$$x^2 - 5x + 6$$
 2. $x^2 - 9x - 10$

Standard Form and Factoring

Practice: Factor. Write Prime for any that cannot be factored.

Algebra

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1. $x^2 + 8x + 12$ 2. $x^2 + 8x + 15$ 3. $x^2 + 10x + 24$ 4. $x^2 + 10x + 9$ 5. $x^2 + 8x - 33$ 6. $x^2 - 4x + 5$ 7. $x^2 + 16x - 36$ 8. $x^2 - 5x + 4$

Practice: Factor. Write Prime for any that cannot be factored.

1. $x^2 - 8x + 7$ 2. $x^2 - 7x - 30$ 3. $x^2 + x - 30$ 4. $x^2 + 19x - 42$ 5. $x^2 - 2x + 1$ 6. $x^2 - 3x + 4$ 7. $x^2 + 7x + 10$ 8. $x^2 - x - 2$

Factoring: GCF with 'Easy Ones'

Examples: Factor completely. Begin by factoring out the GCF. Finish by using reverse FOIL.

$$2x^3 - 10x^2 + 8x$$

$$2x^2y - 14xy + 24y$$

Practice: Factor Completely.

- 1. $5x^2 + 40x + 60$ 2. $x^5 + 8x^4 + 15x^3$
- 3. $ax^2 + 10ax 24a$ 4. $3x^2 + 39x + 90$
- 4. $3x^2 + 39x + 90$
- 5. $2x^3 + 10x^2 72x$ 6. $-x^2y^2 13xy^2 + 30y^2$

Practice: Factor. Write Prime for any that cannot be factored.

1. $3x^2 - 24x + 21$ 2. $x^3 - 2x^2 + x$ 5. $-14x^2 + 28x - 14$ 6. $5x^2 - 65x - 150$ 7. $9x^2 + 63x + 90$ 8. $-24x^2y + 24xy + 48y$

Name_

Period_

Algebra

Factoring 'Easy Ones' with GCFs

Factor eact expression by first factoring the GCF and then using reverse FOIL. Write Prime for any that cannot be factored.

1.
$$4x^2 - 4x - 24$$
2. $2x^2 - 28x + 98$ 3. $-5x^2 - 35x - 60$ 4. $x^2y - 18xy + 17y$ 5. $9x^2 + 36x - 108$ 6. $6x^2y - 12xy - 48y$ 7. $10x^3 - 30x^2 - 100x$ 8. $2x^2 + 4x - 70$ 9. $7x^2 + 49x + 42$ 10. $-2x^2 - 6x + 20$

11. $x^2 y^2 - xy^2 - 72y^2$ **12.** $9x^2 + 27x - 36$

13. $-3x^2 + 6x - 3$ 14. $ax^2 + 32ax + 31a$

Factoring: Difference of SquaresAlgebra9.7Examples: Factor completely. $x^2 - 9$ $25x^2 - 49$ $x^4 - 36$

Practice: Factor Completely.

- 1. $x^2 1$ 2. $9x^2 121$ 3. $x^8 25$
- 4. $100x^2 169$ 5. $9x^4 1$ 6. $2x^2 50$

You can factor out the GCF first.

Examples: Factor completely.

 $x^3 - 25x = 16x^2 - 100 = 3x^4 - 27$

Practice: Factor Completely.

- 1. $5x^2 45$ 2. $4xy^2 36x$
- 3. $x^7 x$ 4. $x^3 y^3 4xy$
- 5. $6x^5 6x$ 6. $-4x^2 + 64$

Examples: Factor completely.

$$x^2 - 6x + 9$$
 $25x^2 - 70x + 49$

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Practice: Factor Completely.

- 1. $x^2 10x + 25$ 2. $x^2 + 16x + 64$
- 3. $4x^2 + 12x + 9$ 4. $x^4 + 14x^2 + 49$

Recognizing Perfect Squares:

Don't be fooled by these imposters! Only one is a perfect square. Can you find it? Factor and Check!

1. $x^{2} - 14x - 49$ 2. $4x^{2} + 18x + 81$ 3. $25x^{2} - 20x + 4$ 4. $9x^{4} - 6x + 1$

Easy Ones, Perfect Squares, and Difference of Squares: Put it all together. Try to recognize how to factor each.

- 1. $2x^2 16x 40$ 2. $a^2 81$
- 3. $x^2 6x + 5$ 4. $17x^2 34x 51$

	Name	Period
Factoring and FOIL Review Multiply (FOIL or Grid method)	A	lgebra
1. $(x^2 - 3x + 1)(x + 5)$	1	
2. $(4a-3)^2$	1.	
3. $(3x-2)(x-y)$	2.	
4. $(12x^3 - 7)(12x^3 + 7)$	3.	
	4.	
Factor Each Completely (Look for GCFs, Perfect Squares, and Difference of S Write PRIME for any that cannot be factored.)	Squares.	
5. $x^2 - 13x - 30$	5.	
6. $x^4 - 16$	6	
7. $x^2 - 9x + 20$	7	
8. $x^3 - 3x^2 + 18x$	8	
9. $x^2 + 17x + 42$	0.	
10 . $3x^2 - 27$	7.	
11. $9x^2 - 30x + 25$	10.	
12. $3x^4 - 39x^2 + 108$	11.	
	12.	

Name_

Period _____

Algebra

Factoring Practice

Challenge 1: Factor <u>Completely.</u>

 $256x^8y - y^9$

Ch. 1. _____

Challenge 2:

The number 65,535 is equal to 2^{16} - 1. Use what you know about a difference of squares to find the four prime factors of 65,535 without a calculator (be ready to explain how this can be done).

Ch. 2. _____

	Name	Period
Factoring and FOIL Pract Multiply (FOIL or Grid method)	ice Quiz	Algebra
1. $(a^2 - b)(a + 2b - 3)$		1
2. $(2x-5)^2$		2
3. $(3x - y)(3x + y)$		3
4. $(x^3 - 2)(2x + 3)$		4
Factor Each Completely (Look for GCFs, Perfect Squares, and Differenc Write PRIME for any that cannot be factored.)	e of Squares.	
5. $x^2 - 13x - 30$		5
6. $121a^2 - b^2$		6
7. $x^2 - 19x + 48$		7

	Name	Period
Factoring and FOIL Practice Factor Each Completely (Look for GCFs, Perfect Squares, and Difference of S Write PRIME for any that cannot be factored.)	e Quiz Alg	ebra
$8. x^2 y - 8xy + 15y$	8	
9. $x^2 - 12x + 11$	9	
10. $5x^2 + 15x$	10	
11. $25x^2 - 40x + 16$	11	
12. $2x^2 + 2x - 40$	12	
13. $x^4 - 81$	13	
14. $144x^2 - 24x + 1$	14	

Name

Factoring and FOIL Self-Check

Factor each (Look for perfect squares and difference of squares, GCF, and easy ones).

 1. $x^2 - 6x + 9$ 2. $x^2y - 5xy + 6y$

 3. $9x^2 - 49$ 4. $x^2 - 7x - 30$

 5. $4x^2 - 28x + 49$ 6. $4x^2 - 64$



Period ____

Algebra

Factoring Review.

Algebra 9.7

Easy Ones: Factor completely. Write *PRIME* for any that cannot be factored.

Ex.:
$$x^{2} - 9x + 20$$

1. $x^{2} + 6x - 16$
2. $x^{2} - 3x - 28$
3. $x^{2} - 25x - 54$
4. $3x^{2}y + 12xy - 15y$

Difference of Squares: Factor completely. Write *PRIME* where applicable. Ex.: $16x^2 - 9$

- 1. $49 x^2 144$ 2. $x^2 100$
- $ax^2 ay^2$ $ax^2 + 36$

Perfect Squares: Factor completely. Write *PRIME* where applicable. Ex.: $x^2 - 10x + 25$ 1. $x^2 + 8x + 16$ 2. $4x^2 - 40x + 100$

3. $x^2 - 2x - 1$ 4. $25x^2 + 60xy + 36y^2$

Hard Ones 'Magic Number'

Look at the trinomial below. Is there a GCF to be factored? Is it an 'Easy One', a Perfect Square, or a Difference of Squares?

 $4x^2 - 16x + 15$

The answer to all of these questions is "No." We will call this type of factoring the 'Magic Number' Method.

Example: Factor
$$4x^2 - 16x + 15$$

- 1. Find/Factor the Magic Number.
- 2. Rewrite the middle term.
- 3. Regroup.
- 4. Factor out the GCFs.

2. $4x^2 + 13x + 10$

5. Finish (___)(___)

Two more examples. Watch Carefully!

1. $3x^2 + 11x - 20$ 2. $10x^2 - 9x + 2$

Practice: Factor each completely.

1. $9x^2 - 3x - 2$

Practice: Factor each completely.

1. $25x^2 + 20x + 4$ 2. $3x^2 - 30x + 27$

Hard Ones 'Magic Number'

Look at each trinomial below. DO NOT TRY TO FACTOR THEM. Label each with: EASY ONE DIFFERENCE OF SQUARES PERFECT SQUARE HARD ONE (MAGIC NUMBER)

(hint: there are two of each)

- 1. $x^2 + 4x 5$ 2. $81x^2 72x + 16$
- 3. $x^2 144$ 4. $5x^2 46x + 9$
- 5. $x^2 + 22x + 40$
- 7. $16x^2 + 56x + 49$
- 6. $x^2 y^2 9$
- 8. $3x^2 + 25x 18$

Now, try to factor them.

- 1. $x^2 + 4x 5$
- 3. $x^2 144$
- 5. $x^2 + 22x + 40$

7. $16x^2 + 56x + 49$

- 2. $81x^2 72x + 16$
- 4. $5x^2 46x + 9$
- 6. $x^2 y^2 9$
- 8. $3x^2 + 25x 18$



Name_

Factoring Review

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Period ____

Factor each: Write Prime for any that cannot be factored.

1.
$$x^2 - 14x + 49$$
 2. $x^2 + 3x - 28$

3.
$$10x^2 + 11x - 6$$
 4. $25x^2 - y^2$

5.
$$9x^2 - 12x + 4$$
 6. $9 - x^2$

7. $x^2 - 4x + 3$ 8. $8x^2 - 22x - 21$

Period ____ Name____ Algebra **Factoring Review** 9.7 Factor each: Write Prime for any that cannot be factored. 10. $x^2 - 18x + 77$ 9. $x^2 - 21x + 54$ 12. $81x^2 - 121y^2$ 11. $4x^2 - 14x + 49$ 14. $4x^2y^2 - 81$ 13. $12x^2 - 11x - 5$ 15. $2y^2 - 5xy + 2x^2$ 16. $x^4 - 2x^2y^2 + y^4$

Factoring Quiz ReviewAlgebra 9.7Factor each: Write Prime for any that cannot be factored.100.
$$x^2 - 16$$
200. $x^2 - 3x - 54$ 300. $12x^2 - 25x + 12$ 400. $6x^2 - 21xy + 9y^2$

Factor each: Write Prime for any that cannot be factored.

 100. $169 - x^2$ 200. $x^2 - 19x + 48$

 300. $x^6 - x^2$ 400. $2x^2y^2 - 9xy + 9$

Factor each: Write Prime for any that cannot be factored.

100. 7x - 49 200. $25x^2 - 10x + 1$

300. $10x^2 + 11x - 8$ 400. $x^4 - 5x^2 + 4$

2. $(3a+1)(3a-1)$	2
3. $(3x + y)(2y - x)$	3
Factor each COMPLETELY NONE OF THE PROBLEMS BELOW ARE PRIME. (Look for perfect squares and difference of squares, easy ones and hard	l ones).
4. $9x^2 - y^2$	4
5. $a^3 - 9a$	5
6. $x^2 - 17x + 60$	6
7. $2x^2 - 10x + 12$	

2.
$$(3a+1)(3a-1)$$

1. $(x-3)^2$

- 3. (

Factoring and FOIL Practice Quiz

Multiply each (Look for perfect squares and difference of squares, order the terms by descending powers of x):

Name_



1. _____

7. _____

Period ____

Name_

Factoring and FOIL Practice Quiz

Factor each COMPLETELY

Write PRIME for any that cannot be factored. (Look for perfect squares and difference of squares, easy ones and hard ones).

8.
$$25x^2 - 100y^2$$

8. ______
9. $4x^2 - 36x + 81$
9. ______
10. $x^2 - 3x + 40$
10. ______
11. $10x^2 - 39x + 14$
11. _____
12. $x^4 - 2x^2y^2 + y^4$
12. _____

Period _

9.8

Algebra

Simplifying Expressions
 Algebra

 Practice: Factor each.
 1.
$$x^2 + 3x$$
 2. $x^2 - 9$
 3. $2x^2 + x - 15$

 Now, try to simplify the following:
 1. $\frac{x^2 + 3x}{x^2 - 9}$
 2. $\frac{x^2 - 9}{2x^2 + x - 15}$
 3. $\frac{2x^2 + x - 15}{x^2 + 3x}$

Practice: Simplify each expression.

1.
$$\frac{x(x+7)}{(x+7)(x+2)}$$
 2. $\frac{x^2 - 9x + 20}{x^2 + x - 20}$

Practice: Simplify each expression.

1.
$$\frac{x^2 - 25}{x^2 - 10x + 25}$$
 2. $\frac{x^2 - 5x + 4}{2x^2 - 9x + 4}$

Practice: Simplify each expression.

1.
$$\frac{2x(x-3)(x+3)}{x(x+3)(x+3)}$$
2.
$$\frac{5x^3 - 10x^2}{3x^2 - 6x + 2}$$

^ ^

$$\frac{6x^2 - 23x + 20}{4x^2 - 20x + 25}$$

$$\frac{x^4 - 18x^2 + 81}{x^2 + 6x + 9}$$

Name_

Period

9.7

Algebra

Simplify by Factoring

Factor each and simplify where possible.

$$\frac{x(x-7)}{(x-7)^2}$$
2. $\frac{x^2+5x+6}{x^2+x-6}$

$$\frac{x^{2} + 12x - 13}{x^{2} - 2x + 1}$$
4. $\frac{x^{2} - 25}{x^{2} - 10x + 25}$

5.
$$\frac{3x^2 - 15x + 12}{3x^2 + 15x + 12}$$
 6. $\frac{5x^2 - 40x + 35}{x^2 - 8x + 7}$

$$\frac{x^{3}-9x^{2}+14x}{x^{3}-4x^{2}+4x} \qquad \qquad \frac{x^{4}-5x^{2}+4}{x^{2}-3x+2}$$



Practice: Solve each.

- 1. 3x + 5 = 5 2. 3(x+5) = 15 3. x(x+3) = 0
- If ab = 0 then either a=0 or b=0. If (x-3)(x+5)=0 then either (x-3)=0 or (x+5)=0.

Examples: Solve each for x. Each will have two solutions.

Solving Equations by Factoring

- 1. x(x+7) = 0 2. (x-9)(x+5) = 0
- 3. $x^2 6x 16 = 0$ 4. $2x^2 7x 15 = 0$

Practice: Solve for x. Each will have two solutions.

1. $x^2 - 3x = 0$ 2. $x^2 + 9x + 20 = 0$ 3. $x^2 - 16 = 0$ 4. $6x^2 + 7x - 10 = 0$

Tricky Examples: Solve each for x.

1. $x^2 - x = 2$ 2. $\frac{1}{5}x^2 + 5 = 2x$

Tricky Practice: Solve each for x.

3.
$$x^2 - 3x = 10$$
 4. $\frac{1}{2}x^2 - x = 12$

	Name	Peri	od
Solving Quadratics by Fact	oring	Algebra	9.7
Factor each and simplify where possible.			

1.
$$(x-3)(x-5) = 0$$

2. $2x^2 - 5x + 2 = 0$

3.
$$x^2 + 12x + 36 = 0$$
 4. $25x^2 - 1 = 0$

5.
$$x^2 - x - 12 = 0$$
 6. $6x^2 - 19x + 10 = 0$

7.
$$9x^2 + 3x - 2 = 0$$

8. $x^2 + 6x = 7$

9.
$$8x^2 + 1 = 6x$$
 Challenge: $x^4 + 9 = 10x^2$ (4 solutions)

Factoring Problems



For the problems below, you must know the Pythagorean Theorem:



In any right triangle:



Example:

Find the lengths of the sides of the right triangle below.



Practice:

Find the lengths of the sides of the right triangle below.



Practice:

- In a right triangle, the hypotenuse is 9 inches longer than the shortest side. The length of the medium side is just one inch longer than the length of the shortest side. What is the perimeter in inches of the triangle?
- 2. The hypotenuse of a right triangle is 1cm longer than the long leg. The short leg is 1cm shorter than half the long leg. What is the triangle's area?

Name	
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Period

Algebra

Solving Quadratics by Factoring

Factor each and simplify where possible.

1.
$$x^2 - 10x + 21 = 0$$
 2. $16x^2 - 9 = 0$

3.
$$x^2 - x = 56$$
 4. $25x^2 + 3 = 20x$

5.
$$9x^2 + 9x = 10$$
 6. $x^2 = 3x + 10$

7.
$$8x^2 = 18x + 5$$

8. $x^3 - 4x = 0$ (3 solutions)

9. The equation $x^2 + kx + 36 = 0$ has only one solution for positive integer k. What is k?

10. Find the perimeter of the triangle below.



Clever Factoring:

Algebra

Some tricks and more difficult problems:

Example:

One of the solutions to the equation $x^2 + a = 6x$ is 5.

- **a.** What is the value of *a*?
- **b.** What is the other solution?

Practice:

- **1.** The equation $3x^2 ax = 8$ has x = 4 as a solution.
 - **a.** What is the value of *a*?
 - **b.** What is the other solution?
- **2.** The equation $ax^2 5x = 2$ has x = 1 as a solution.
 - **a.** What is the value of *a*?
 - b. What is the other solution?

Example:

How can the polynomial $(x + y)^2 - 9$ can be factored into the product of two trinomials?

Practice:

- **1.** Factor the following into a product of trinomials: $(x-2)^2 y^2$.
- **2.** Factor the following into a product of trinomials: $x^2 y^2 10x + 25$.

Solving Trickier Equations Practice:

1. Solve for x: $3(x^2 - 4) - x(x^2 - 4) = 0$.

Hint: Where have you seen something similar to this before?

2. Solve for x: $\frac{10}{x^2} - \frac{9}{x} + 2 = 0$.

Hint: use a common denominator.

3. Solve for x:
$$\frac{x-6}{14-3x} = \frac{3}{x-2}$$
.

Factoring Test Review

Algebra 9.8

Perfect Squares and Difference of Squares: Factor each.

100.
$$9 - x^2$$
 200. $6x^2 - 24$

 300. $2x^2y^2 + 12xy + 18$
 400. $x^4 - 81$

Easy Ones and Magic Number: Write Prime for any that cannot be factored.

100.
$$x^2 - 6x + 8$$
 200. $x^2 - 22x + 72$

300.
$$12x^2 + 5x - 3$$
 400. $6x^2 + xy - 2y^2$

Solve each: Write Prime for any that cannot be factored.

100.
$$\frac{1}{3}x^2 - 30x = 0$$
 200. $x^2 + 24 = 11x$

300.
$$\frac{4}{7}x^2 + 7 = 4x$$

400. $6x^3 = 25x^2 - 14x$

Period_

Factoring and FOIL Practice Test

Factor each COMPLETELY

Write PRIME for any that cannot be factored.

(Look for perfect squares and difference of squares, easy ones and hard ones, and GCF problems).

1.
$$x^{2} - 4y^{2}$$

2. $34x^{2} - 85x$
3. $x^{2} - 13x - 30$
4. $3x^{2} + x + 10$
5. $a^{3} - 4a^{2} + 4a$
6. _____
7. $x^{4} - 11x^{2} - 80$

NamePeriodFactoring & FOIL Practice Test (4)AlgebraSolve for x:Some problems may have more than one solution. List all solutions in the blank provided.8. 3x(x-7) = 0

8. x=	
9. x=	
10. x=	
11. x=	
12.	
13.	
14.	

9.
$$x^2 - 6x + 9 = 0$$

10.
$$10x^2 + 6 = 17x$$

11.
$$x^2 + 72 = 18x$$

Multiply:

12.
$$(5x-4)(x-5)$$

13.
$$(3x^2 - 5x)^2$$

14.
$$(x-2)(x-3)(x+2)$$

Factoring and FOIL Practice Test Algebra Solve for x: Some problems may have more than one solution. List **all** solutions in the blank provided. 8. 3x(x-7) = 08. x=____ 9. $x^2 - 6x + 9 = 0$ 9. x=____ 10. $10x^2 + 6 = 17x$ 10. x= 11. $\frac{1}{6}x^2 + 12 = 3x$ 11. x= Simplify each: 12. $\frac{x^2 - 5x + 6}{x^2 - x - 6}$ 12. 13. $\frac{4x^2 - 36x + 81}{4x^2 - 81}$ 13. _____ 14. $\frac{4x^3 - 10x^2}{5x^2 - 20}$ 14. _____

Name

Period_